

# Digital twinning for ports: from characterization to operations' modelling

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# Outline

- Ports
- Digital Twins in Industry 4.0
- Research questions
- Overview of papers and contributions
- Conclusion
- Future work

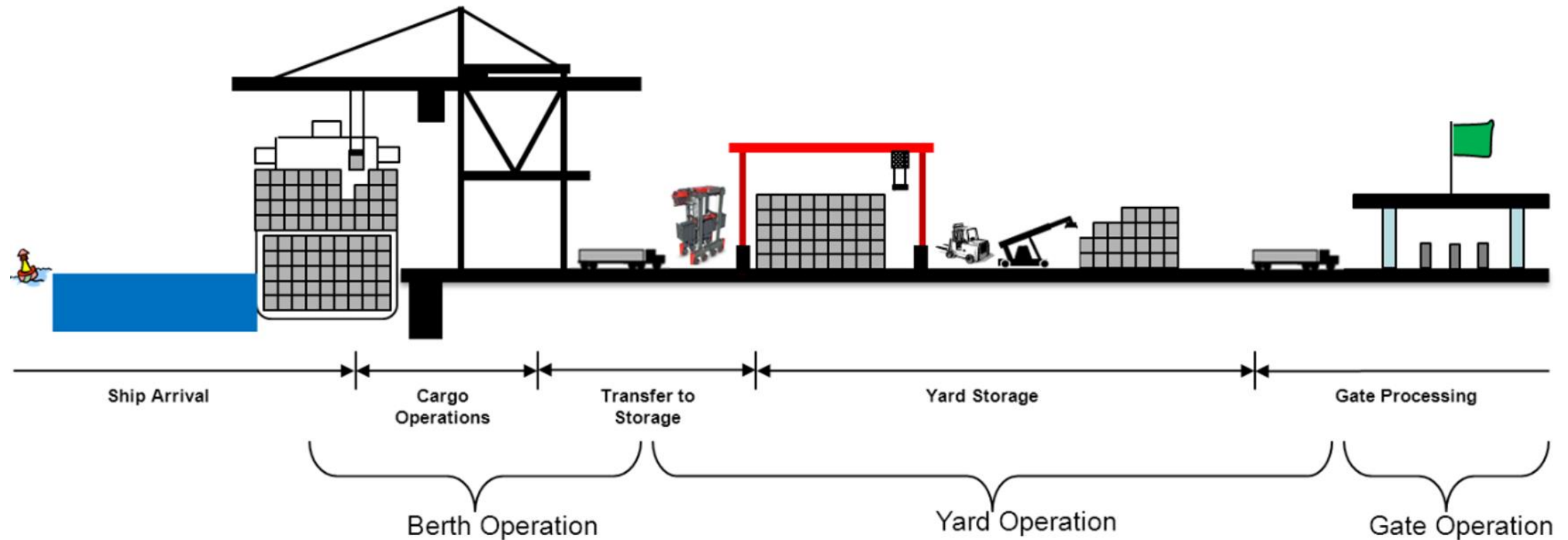
# Ports as part of supply chains

- Multi-modal hubs of trade
  - 90% of world trade passes through ports
- Connect different modes of transport
- Provide temporary storage
  - 80% of containers are temporarily stored
- Accommodate a large number of interlinked processes and actors
- Space, time and cost constraints



Picture taken from VTI ImageVault

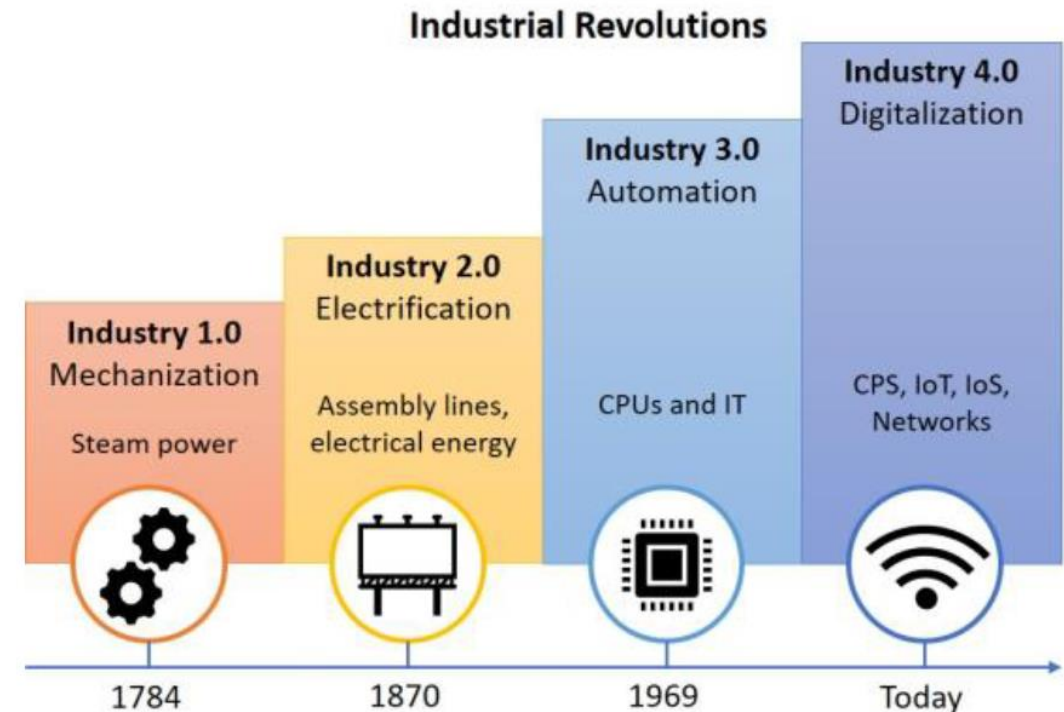
# Overview of ports



International Maritime Organization (IMO) (2016). Module 5 – Ship Port Interface for Energy Efficiency.

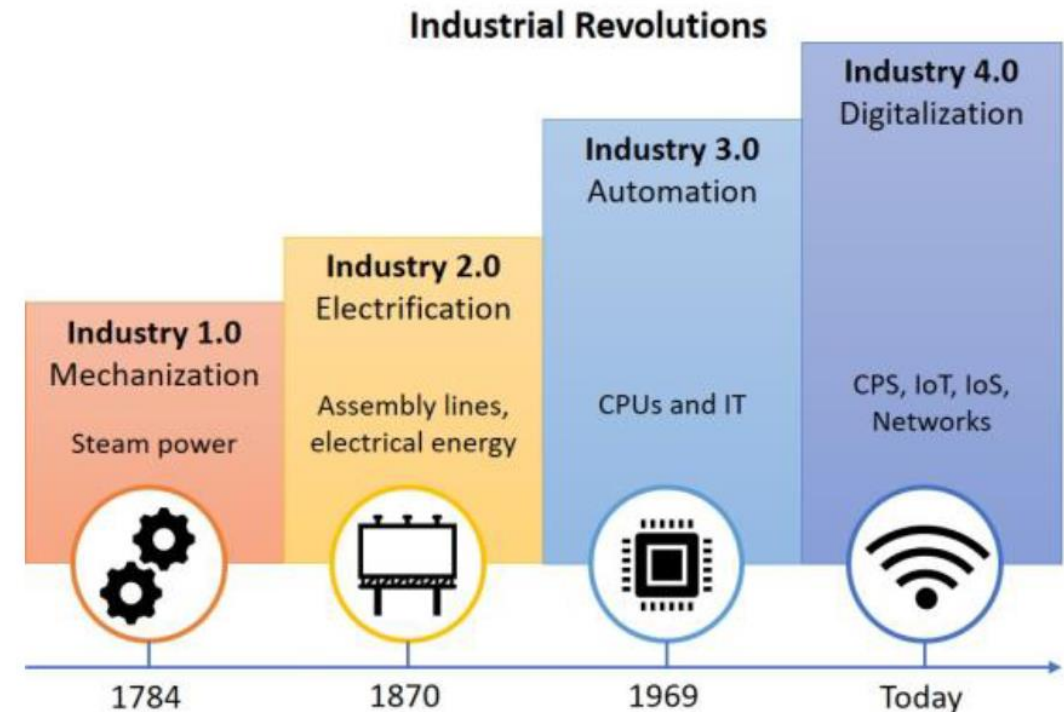
# Digital Twins in Industry 4.0

- Industry 4.0 refers to the wide range of new technologies and digital advances altering production by integrating the physical and virtual worlds



# Digital Twins in Industry 4.0


- Industry 4.0 refers to the wide range of new technologies and digital advances altering production by integrating the physical and virtual worlds
- Digital Twins (DT) clone a physical object into a software counterpart
- Digital Twins considered one of the pillars of Industry 4.0
  - They comprise Industry 4.0 tech such as: CPS, IoT, AI, etc.



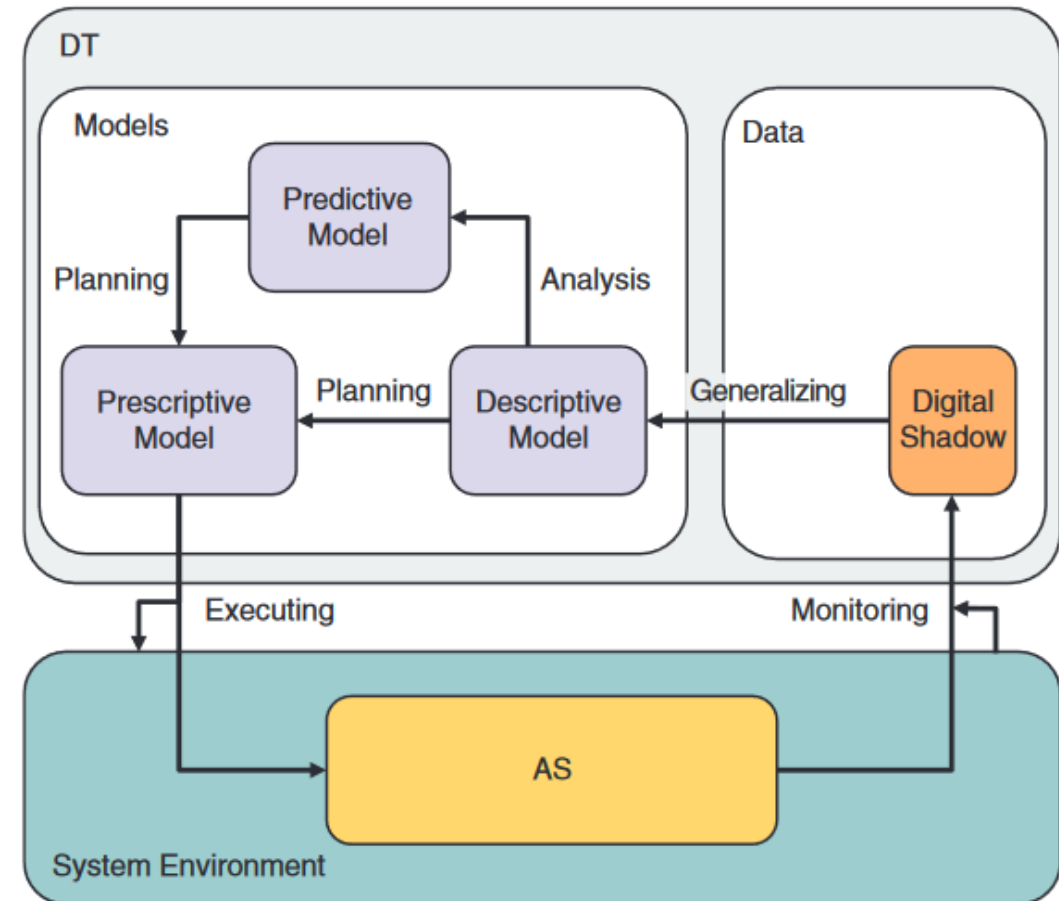


# Digital Twins in Industry 4.0

- “the one” definition of DTs does not exist
- DT solutions share some common characteristics

- 
- Actual Twinned System
  - Virtual Representation
  - (Real Time) Data Collection
  - Modeling
  - Bi-directional data exchange
  - Automation

*... and more in paper 2 of the thesis*



# Research Questions

- **RQ-1:** What are the key characteristics of cross-domain digital twinning solutions, and to what extent can they be transferred to the port?



# Research Questions

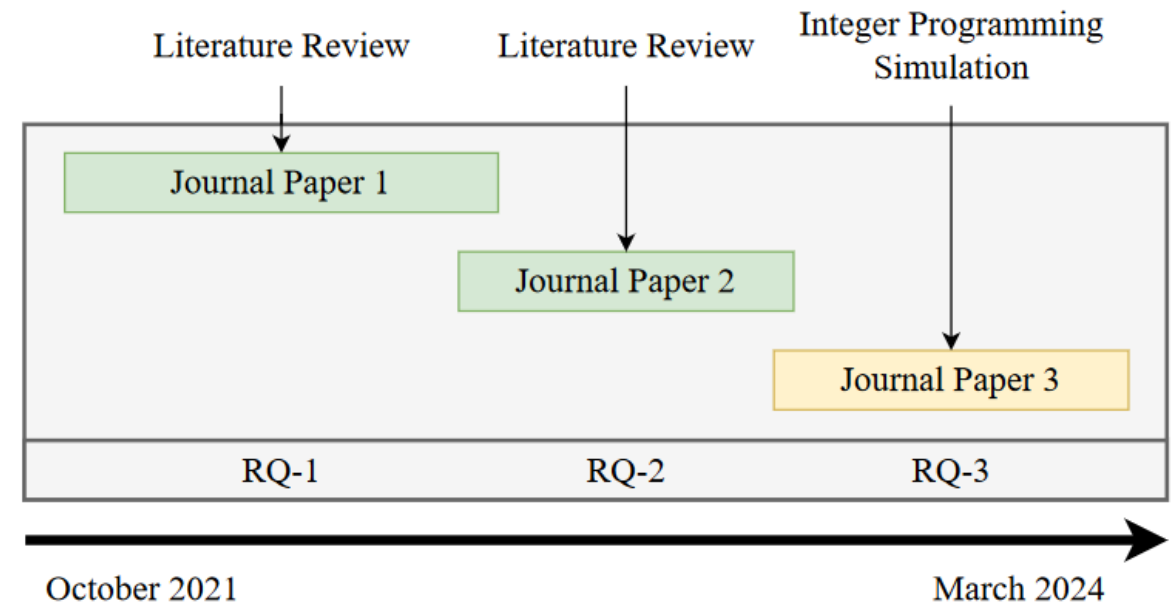
- **RQ-1:** What are the key characteristics of cross-domain digital twinning solutions, and to what extent can they be transferred to the port?
- **RQ-2:** How mature are existing digital twinning solutions in ports and how can their maturity be evaluated?

# Research Questions

- **RQ-1:** What are the key characteristics of cross-domain digital twinning solutions, and to what extent can they be transferred to the port?
- **RQ-2:** How mature are existing digital twinning solutions in ports and how can their maturity be evaluated?
- **RQ-3:** How can digital twin components be designed that could facilitate the effectiveness of multimodal transportation using ports to reduce the carbon footprint of cargo?

# Papers and contributions

- Paper 1
  - Identifies port DT requirements
  - Outlines a port DT
- Paper 2
  - Provides a tool to assess DT maturity
  - Emphasizes the importance of interoperability
- Paper 3
  - Links two important port problems
  - Provides a model suitable for integration into a DT



# Paper 1

## Digital Twins for Ports: Derived From Smart City and Supply Chain Twinning Experience

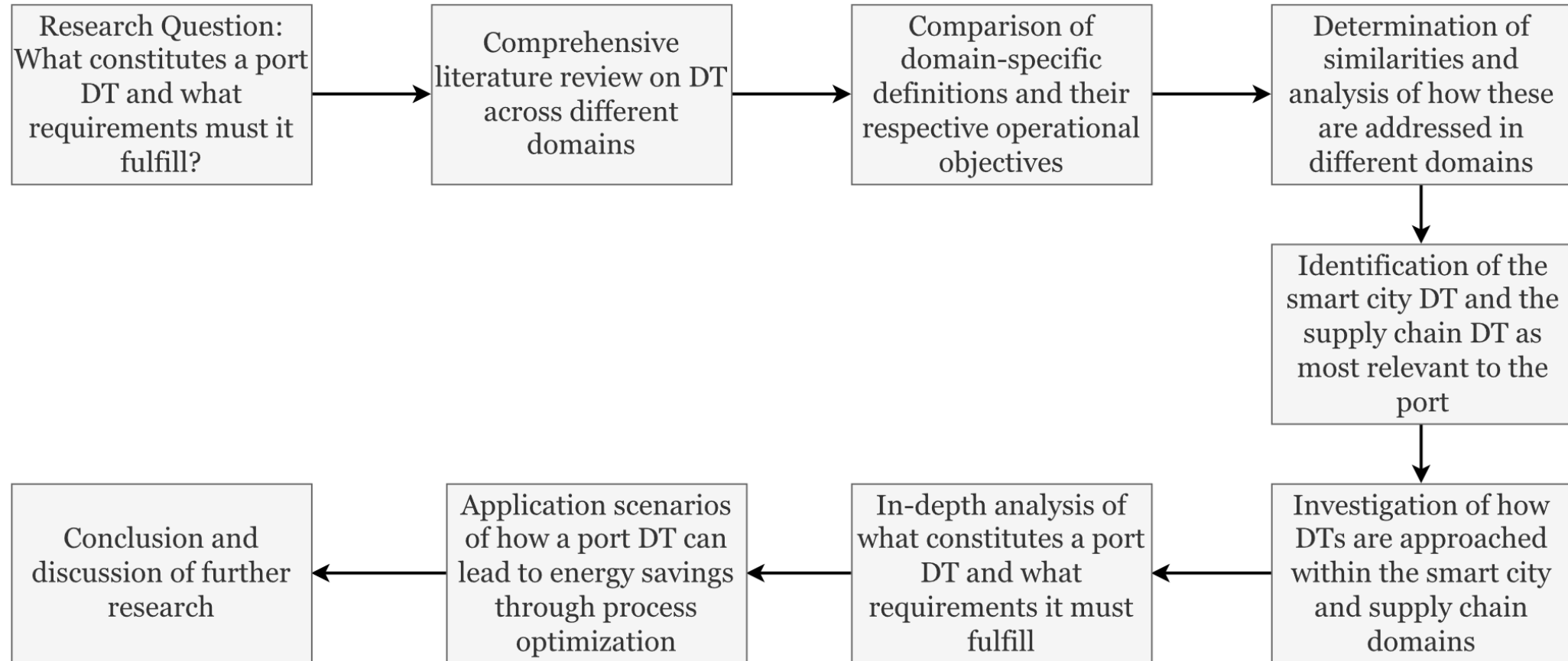
Authors: **Robert Klar**, Anna Fredriksson and Vangelis Angelakis  
in *IEEE Access*, vol. 11, pp. 71777-71799, 2023  
doi: 10.1109/ACCESS.2023.3295495.



# Paper 1: Background

- Lack of research that uses the DT as a tool to optimize the entire port
  - A port is a system of systems
- Existing DT research in ports is limited to twinning assets in isolation
  - E.g., twinning of quay cranes
- Cities and supply chains are very relevant systems of systems
  - Both interact with ports and have more DT-related research
    - How can ports draw from their digital twinning experience? (RQ1)

# Paper 1: Methodology



# Paper 1: Results

- Port DTs are very close to those of smart cities and supply chains
- Key requirements for port DTs:
  - (Real-time) Situational awareness
  - Data-driven (joint) decision making
  - Facilitation of multi-stakeholder governance and collaboration
- A port DT
  - Is a grouping of models and algorithmic components
  - Enables a complete view of past and current operating conditions
  - Allows the prediction of the most efficient operations
  - May act autonomously while providing full transparency across actors



# Paper 2

## Digital Twins' Maturity: The Need for Interoperability

Authors: **Robert Klar**, Niklas Arvidsson and Vangelis Angelakis  
in *IEEE Systems Journal*, vol.18, no.1, pp.713-724, 2024.  
doi: 10.1109/JSYST.2023.3340422.



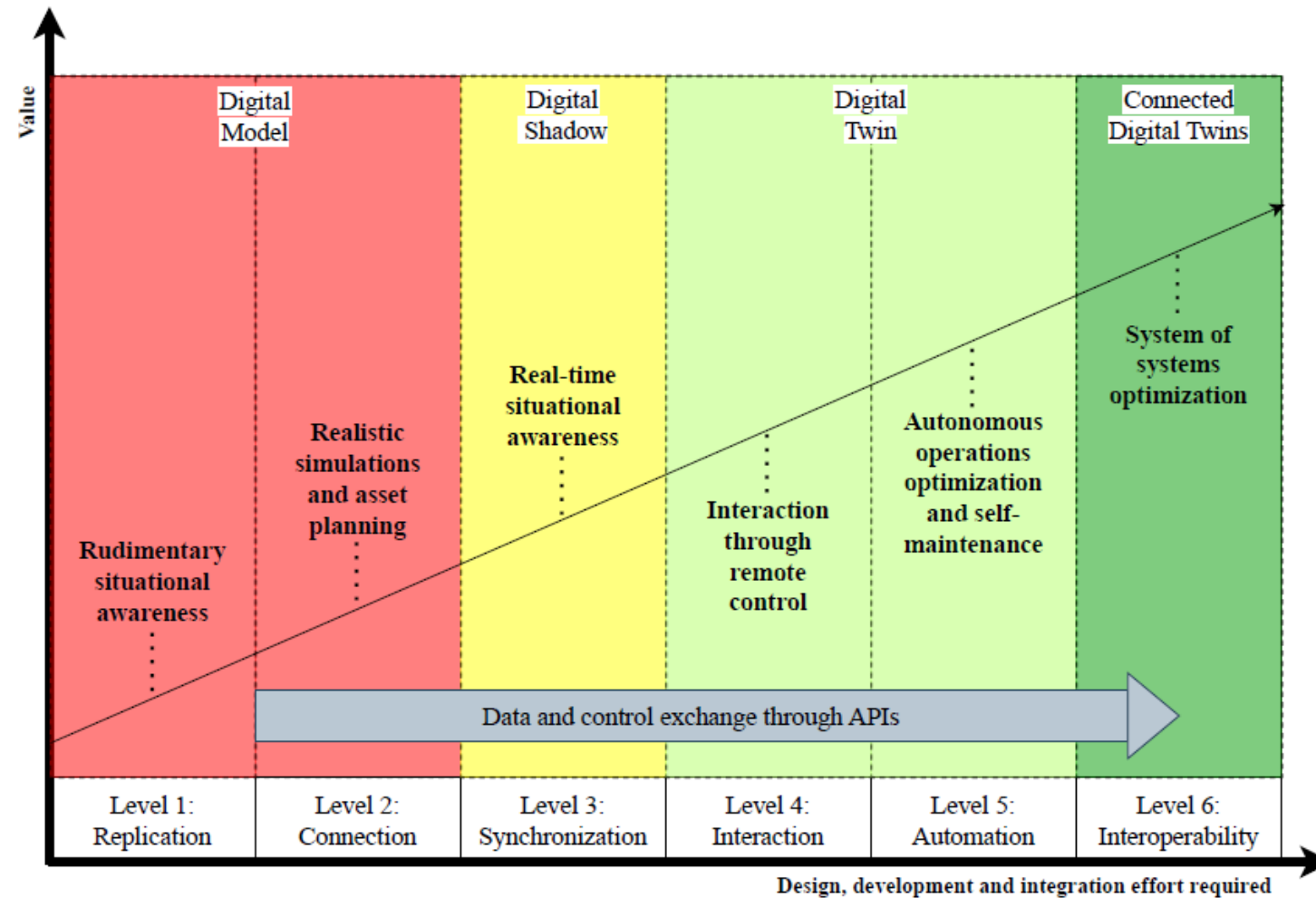
# Paper 2: Background

- Growing number of DT solution providers
  - How to compare and benchmark offerings of different DT solutions? (RQ2)
- Existing DT assessment tools are domain specific
  - There is a lack of domain-independent tools to assess DT maturity
- Most existing DTs act in isolation
  - Interoperability is crucial for system of systems, e.g., ports (RQ2)

# Paper 2: Methodology

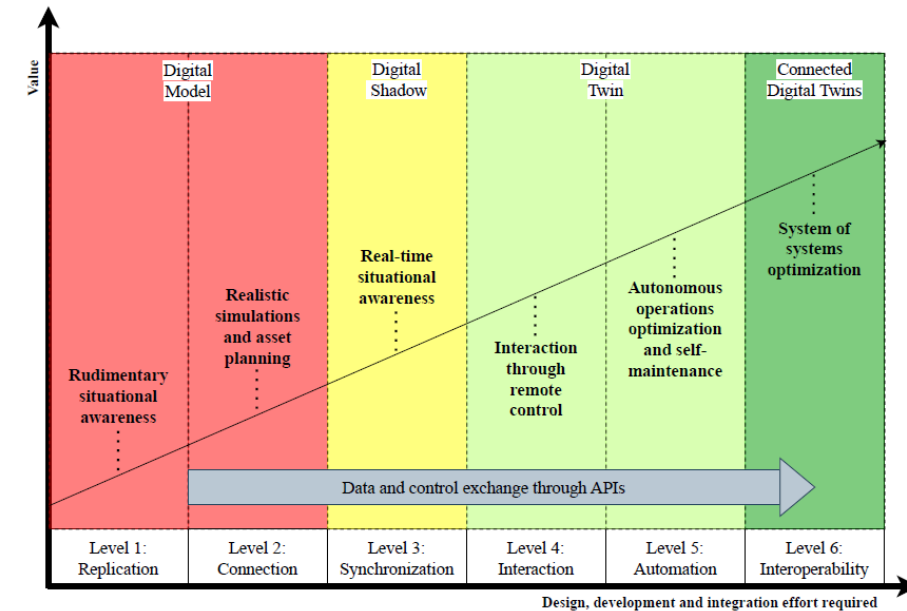
- Systematic literature review to identify
  - Existing domain-specific DT maturity assessment tools
  - Best practices for assessing DT maturity
  - Barriers that hinder the development of DTs towards higher DT maturity
- Maturity characterization derivation
- Application of the derived tool to assessing maturity of existing port DTs

# Paper 2: Results – the tool



# Paper 2: Results – using the tool

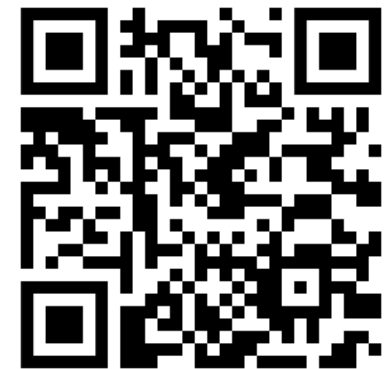
- Innovation-leading ports have already sophisticated DT solutions
- Most ports are still in the initial phase
  - Have maturity level up to 3 (Synchronization)
- Existing DT solutions are restricted by lack of
  - Standardization
  - Trust
- DTs reach full potential through joint decision-making (requires interoperable DTs)



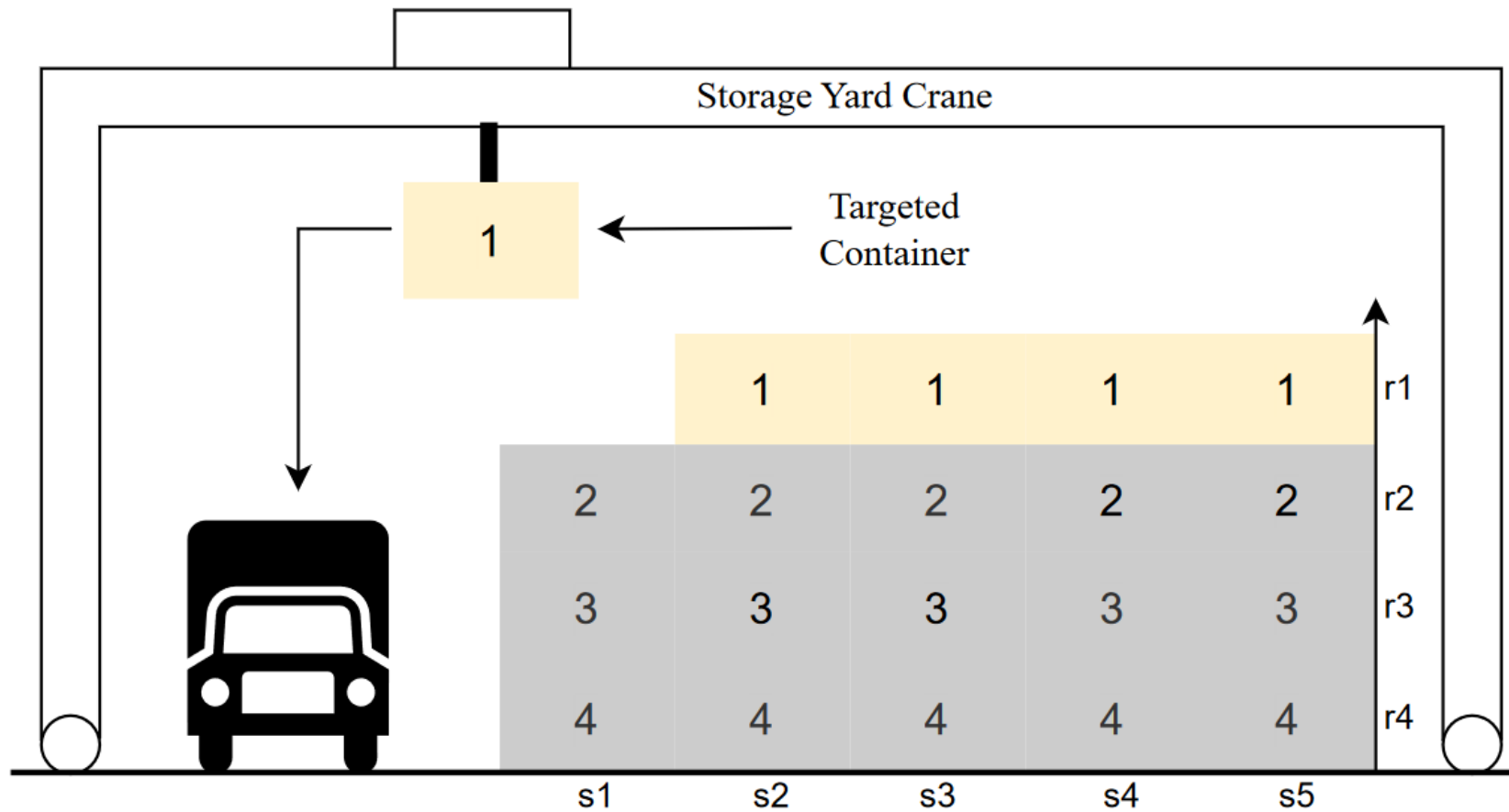
# Paper 3

Container relocation and retrieval tradeoffs  
minimizing schedule deviations and relocations

Authors: **Robert Klar**, Niklas Arvidsson and Vangelis Angelakis  
in *IEEE Open Journal of Intelligent Transportation Systems*,  
vol. 5, pp. 360-379, 2024, doi: 10.1109/OJITS.2024.3413197.

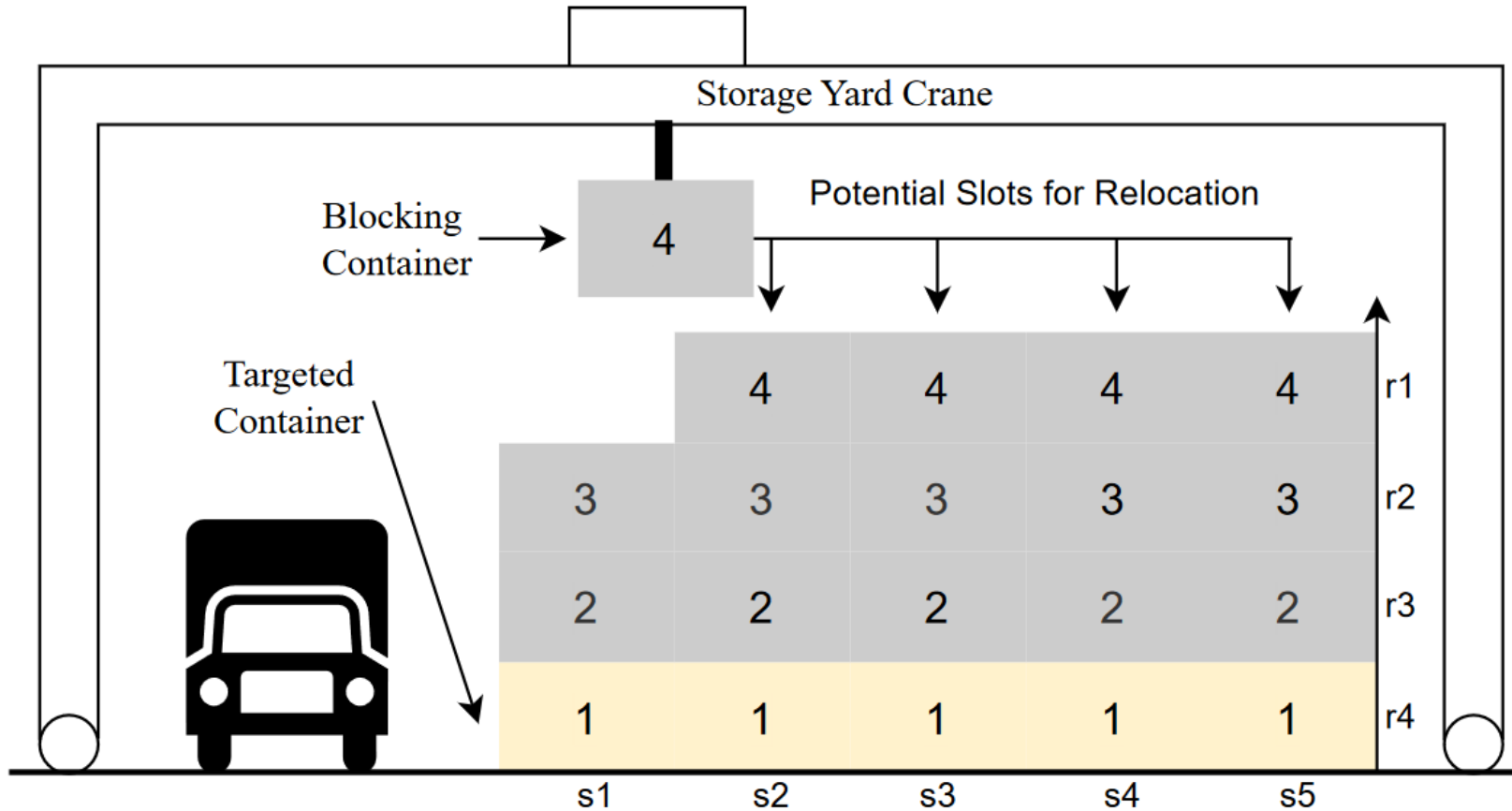


# What we hope for



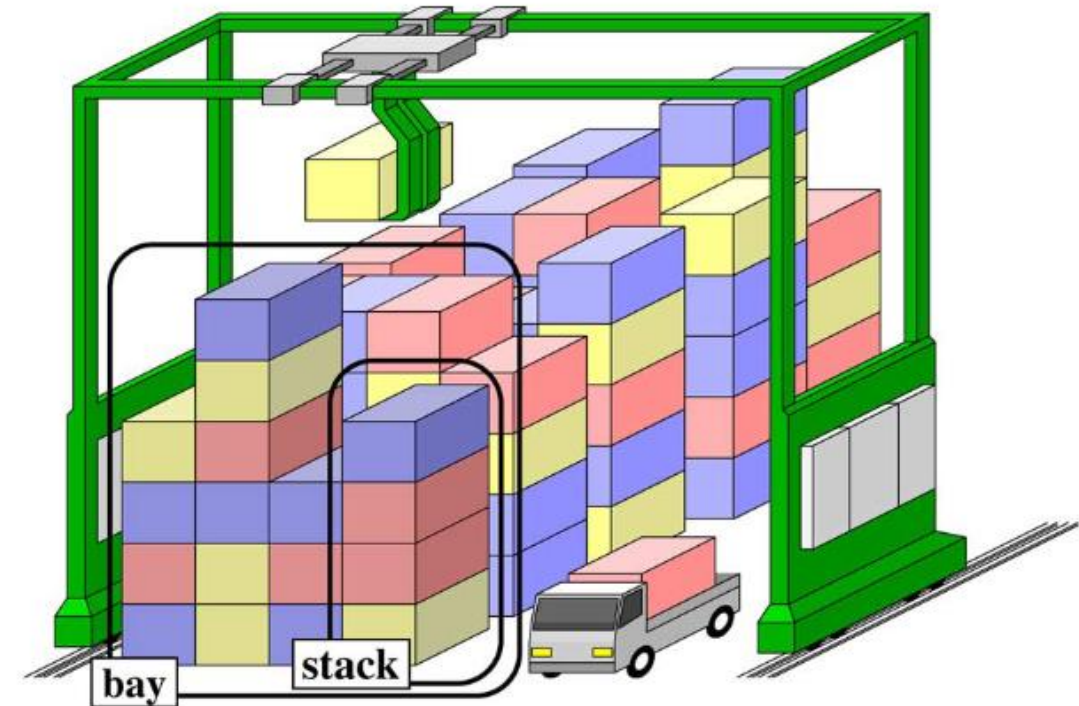


# What occurs in reality

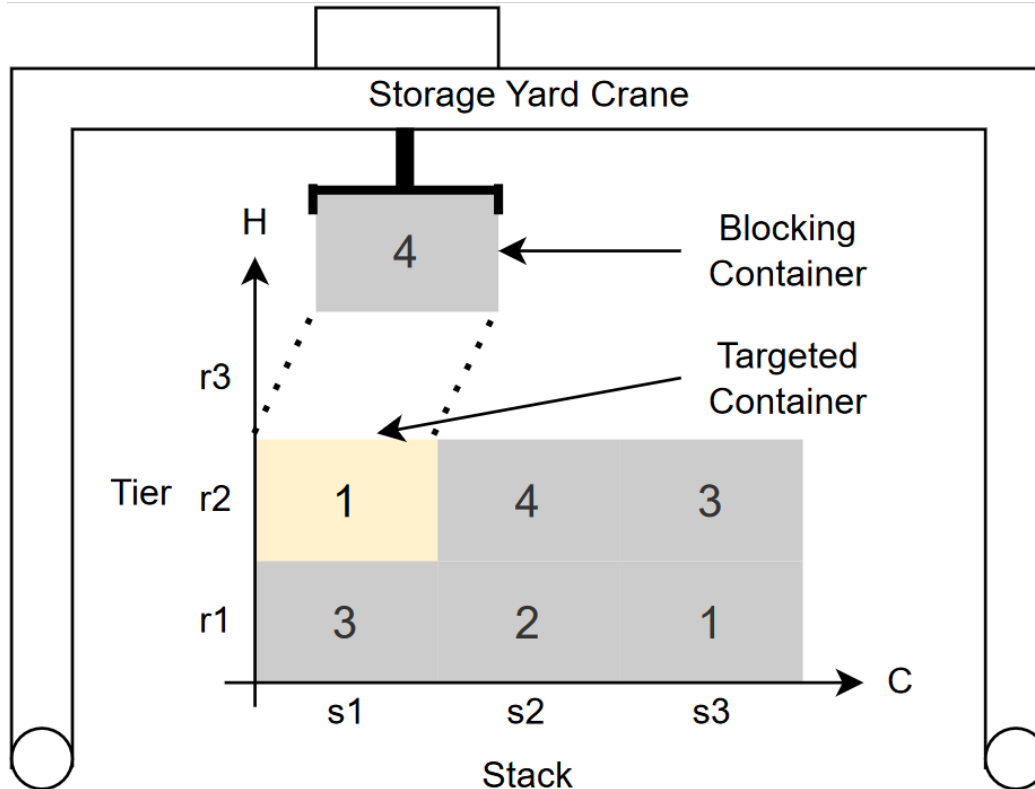


# Background

- Two major challenges in a port storage yard
  - Minimize crane movements (BRP)
  - Maintaining tight truck retrieval schedules
- Existing literature considers each of the problems in isolation
- Improving overall system efficiency requires addressing both jointly



# Block Relocation and Schedule Reliability Problem (BRSRP)



Only the topmost container can be accessed

Current problem configuration:

7 Containers ( $N$ )

3 Stacks ( $C$ ) and 3 Tiers ( $H$ )

4 Time Windows ( $T$ )

In each Time Window  $t \in T$ ,

3 Crane Movements ( $G$ ) are available to serve 2

Trucks ( $L$ )

How can we retrieve all containers while minimizing crane relocations and schedule deviations?

# Problem formulation

BRSRP Model:

$$\begin{aligned} & \text{minimize } z : \\ & \alpha \left( \sum_{i \in N} \left( \sum_{s \in C} \sum_{r \in H} \sum_{k \in G} \sum_{t \in T} ((t - p[i]) \cdot v[i, s, r, k, t]) \right) \right) \\ & + \beta \left( \sum_{i \in N} \sum_{s \in C} \sum_{r \in H} \sum_{k \in G} \sum_{t \in T} y[i, s, r, k, t] \right) \end{aligned} \quad (1)$$

Subject to:

$$p[i] - \sum_{s=1}^C \sum_{r=1}^H \sum_{k=1}^G \sum_{t=1}^T (t \cdot v[i, s, r, k, t]) \leq \delta, \forall i \in \{1, \dots, N\} \quad (2)$$

$$\sum_{s=1}^C \sum_{r=1}^H \sum_{k=1}^G \sum_{t=1}^T (t \cdot v[i, s, r, k, t]) \leq \delta + p[i], \forall i \in \{1, \dots, N\} \quad (3)$$

$$\sum_{i=1}^N \sum_{s=1}^C \sum_{r=1}^H \sum_{k=1}^G v_{isrk}^t \leq L, \forall t \in \{1, \dots, T\} \quad (4)$$

$$\sum_{i=1}^N \sum_{s=1}^C \sum_{r=1}^H v_{isrk}^t + \sum_{i=1}^N \sum_{s=1}^C \sum_{r=1}^H x_{isrk}^t \leq 1, \quad \forall k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (5)$$

$$\sum_{i=1}^N x_{isrk}^t \leq \sum_{i=1}^N (u_{isrk}^t - u_{is(r+1)k}^t), \forall s \in \{1, \dots, C\}, \quad r \in \{1, \dots, H-1\}, k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (6)$$

$$\sum_{s'=1, s' \neq s}^N \sum_{r=1}^H v_{is'r k}^t \geq \sum_{r=1}^H x_{isrk}^t, \forall i \in \{1, \dots, N\}, \quad s \in \{1, \dots, C\}, k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (7)$$

$$\sum_{i=1}^N v_{isrk}^t + \sum_{i=1}^N y_{isrk}^t + \sum_{i=1}^N x_{isrk}^t \leq 1, \quad \forall s \in \{1, \dots, C\}, k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (8)$$

$$u_{isrk}^1 = I_{isr}, \forall i \in \{1, \dots, N\}, s \in \{1, \dots, C\}, \quad r \in \{1, \dots, H\} \quad (9)$$

$$u_{isrk+1}^t = u_{isrk}^t + y_{isrk}^t - x_{isrk}^t - v_{isrk}^t, \quad \forall i \in \{1, \dots, N\}, s \in \{1, \dots, C\}, r \in \{1, \dots, H\}, \quad k \in \{1, \dots, G-1\}, t \in \{1, \dots, T\} \quad (10)$$

$$u_{isr1}^t = u_{isrG}^{t-1} + y_{isrG}^{t-1} - x_{isrG}^{t-1} - v_{isrG}^{t-1}, \quad \forall i \in \{1, \dots, N\}, s \in \{1, \dots, C\}, \quad r \in \{1, \dots, H\}, t \in \{2, \dots, T\} \quad (11)$$

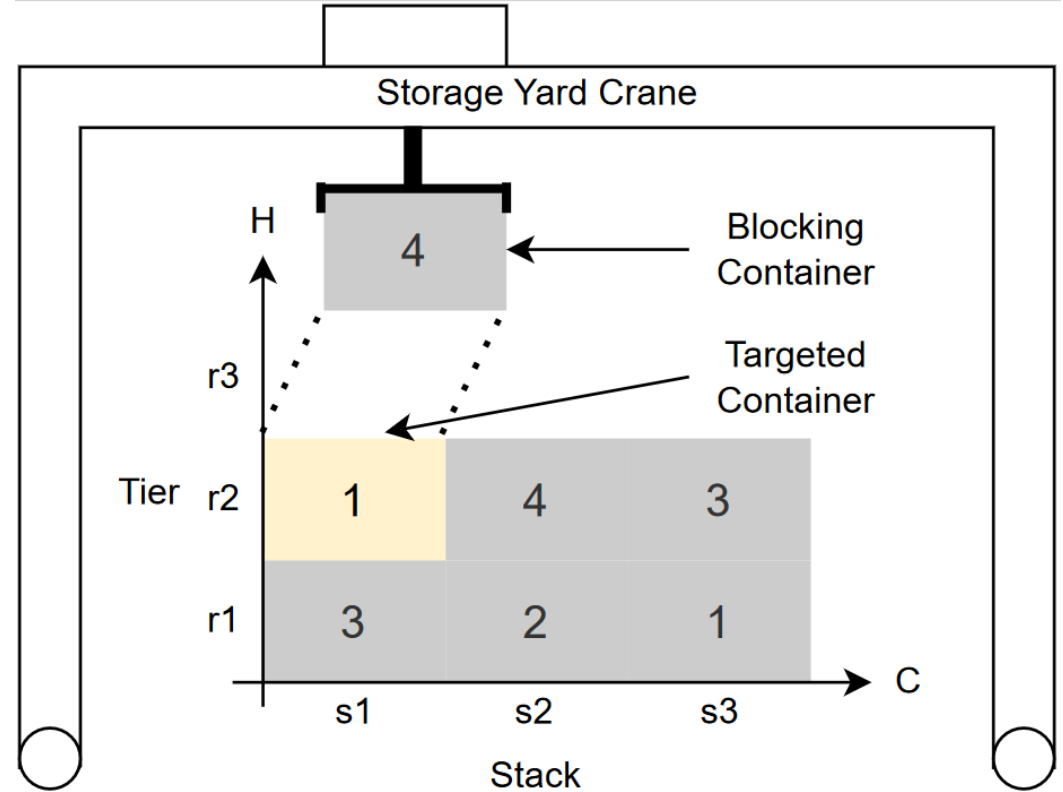
$$\sum_{i=1}^N \sum_{r=1}^H \sum_{k'=k+1}^G u_{isrk'}^t + \sum_{i=1}^N \sum_{r=1}^H \sum_{k'=k+1}^G \sum_{t'=t+1}^T u_{isrk'}^{t'} \leq G * T(1 - \sum_{s=1}^C \sum_{r=1}^H v_{isrk}^t), \quad \forall i \in \{1, \dots, N\}, k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (12)$$

$$\sum_{s=1}^C \sum_{r=1}^H \sum_{k=1}^G \sum_{t=1}^T v_{isrk}^t = 1, \forall i \in \{1, \dots, N\} \quad (13)$$

$$\sum_{i=1}^N u_{isrk}^t \leq 1, \forall s \in \{1, \dots, C\}, r \in \{1, \dots, H\}, \quad k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (14)$$

$$\sum_{s=1}^C \sum_{r=1}^H u_{isrk}^t \leq 1, \forall i \in \{1, \dots, N\}, k \in \{1, \dots, G\}, \quad t \in \{1, \dots, T\} \quad (15)$$

$$u_{isrk}^t, x_{isrk}^t, y_{isrk}^t, v_{isrk}^t \in \{0, 1\}, \quad \forall i \in \{1, \dots, N\}, s \in \{1, \dots, C\}, r \in \{1, \dots, H\}, \quad k \in \{1, \dots, G\}, t \in \{1, \dots, T\} \quad (16)$$



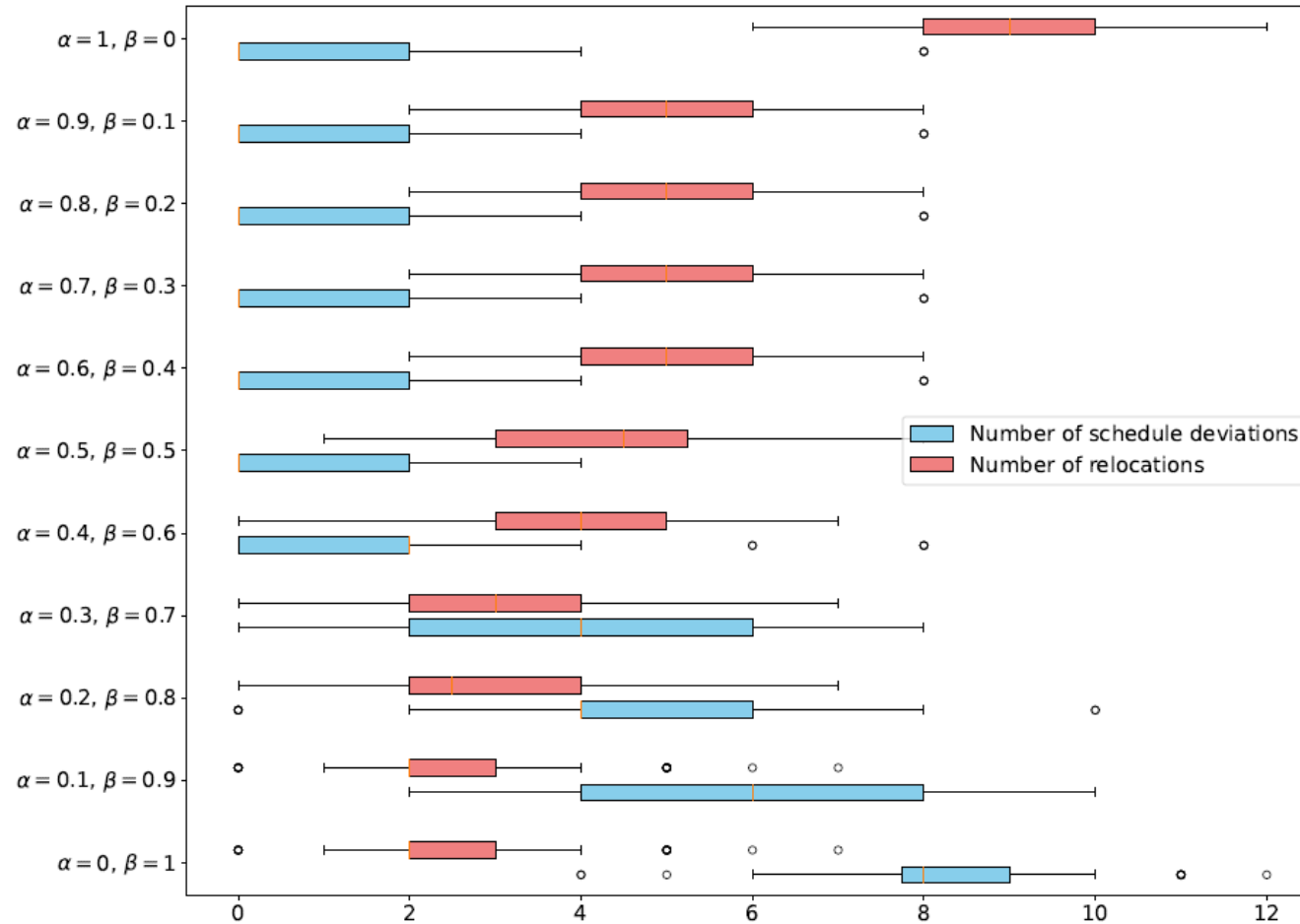
# Problem formulation – Objective Function

	Notation	Explanation
Parameters	$N$	Number of containers in the initial configuration of the bay
	$C$	Number of stacks
	$H$	Maximum allowed height of bay
	$G$	Maximum allowed container moves (either retrievals or relocations) per time window
	$L$	Maximum queue length at bay (appointments per time window)
	$T$	Number of time windows
	$p_i$	Scheduled container pickup time window, $i \in 1, \dots, N$
Indices	$\delta$	Maximum allowed container pickup time window shift
	$I_{isr}$	Whether container $i$ occupies slot $(s,r)$ in the initial bay layout, $I_{isr} \in 0, 1$
	$i$	Index of container, $i \in 1, \dots, N$
	$s$	Index for stack, $s \in 1, \dots, C$
	$r$	Index for tier, $r \in 1, \dots, H$
	$k$	Index of the stage, $k \in 1, \dots, G$ where each stage $k$ represents one possible container move
Variables	$t$	Index for time window, $t \in 1, \dots, T$
	$u_{isrk}^t$	$\begin{cases} 1, & \text{if container } i \text{ occupies the slot } (s, r) \text{ at stage } k \text{ of time window } t \\ 0, & \text{otherwise} \end{cases}$
	$x_{isrk}^t$	$\begin{cases} 1, & \text{if container } i \text{ is relocated from slot } (s, r) \text{ at stage } k \text{ of time window } t \\ 0, & \text{otherwise} \end{cases}$
	$y_{isrk}^t$	$\begin{cases} 1, & \text{if container } i \text{ is relocated to slot } (s, r) \text{ at stage } k \text{ of time window } t \\ 0, & \text{otherwise} \end{cases}$
	$v_{isrk}^t$	$\begin{cases} 1, & \text{if container } i \text{ is picked up from slot } (s, r) \text{ at stage } k \text{ during time window } t \\ 0, & \text{otherwise} \end{cases}$

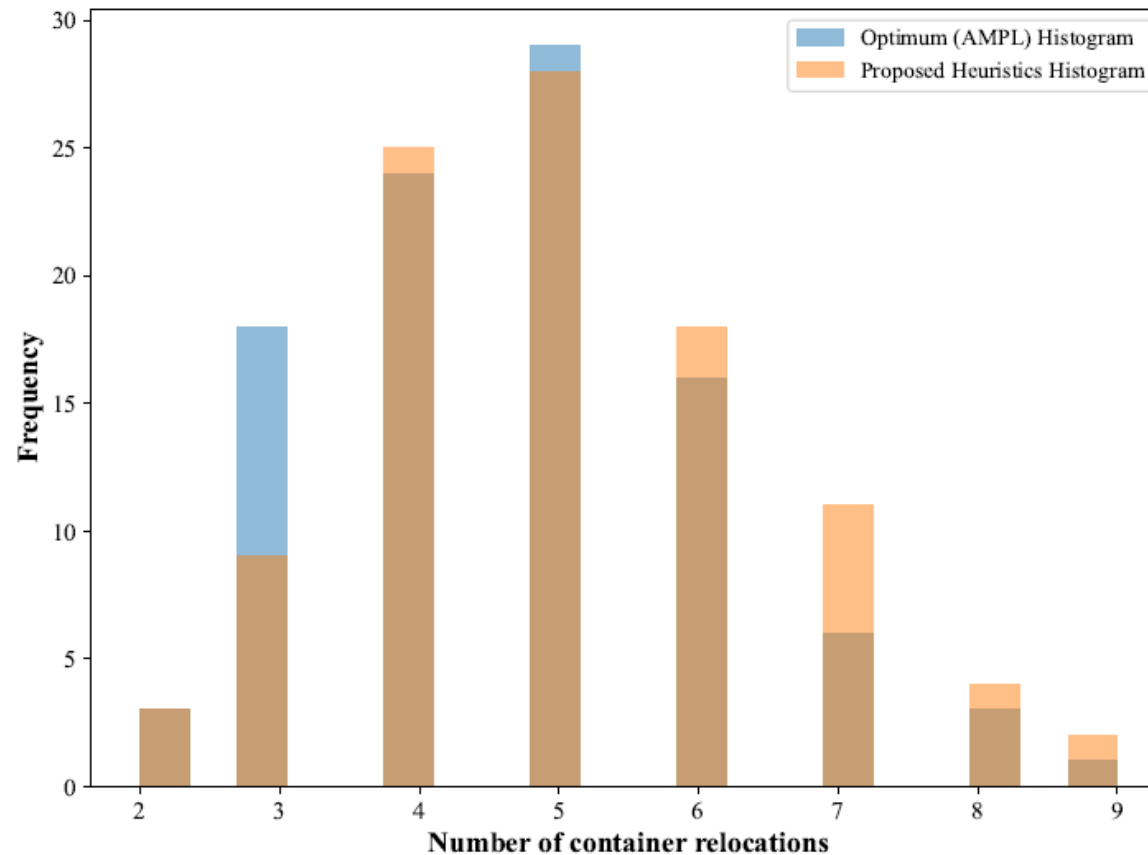
$u_{isrk}^t, x_{isrk}^t, y_{isrk}^t, v_{isrk}^t$  are the decision variables.

$$\begin{aligned} & \text{minimize } z : \\ & \alpha \left( \sum_{i \in N} \left( \sum_{s \in C} \sum_{r \in H} \sum_{k \in G} \sum_{t \in T} (|t - p[i]|) \cdot v[i, s, r, k, t] \right) \right) \\ & + \beta \left( \sum_{i \in N} \sum_{s \in C} \sum_{r \in H} \sum_{k \in G} \sum_{t \in T} y[i, s, r, k, t] \right) \end{aligned}$$

# Results – impact of ( $\alpha, \beta$ ) weights



# Paper 3: Results –exact vs. heuristic



**Example run time for 15 containers:**

Exact solution: 199.9 seconds  
Heuristic solution: 0.019 seconds

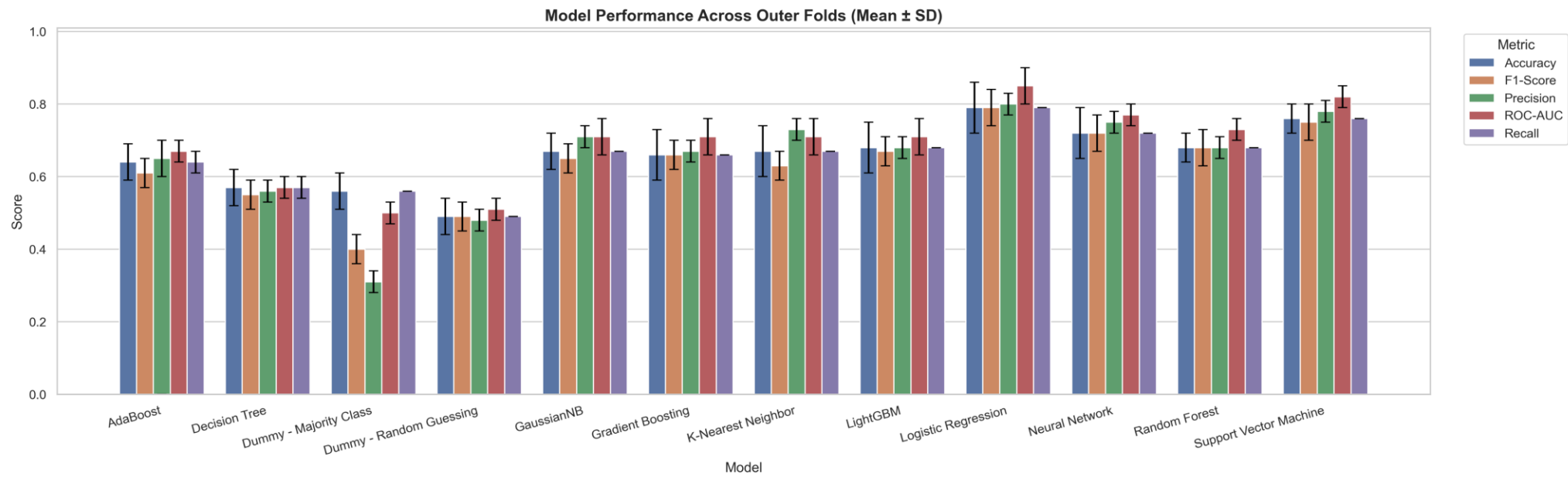


# Conclusion

- From a port perspective, this thesis provides:
  - An overview of the potential, challenges, and practical use cases of how digital twins lead to overall port efficiency
  - A tool for DT users (ports) to assess the maturity future and current DTs
  - A multi-objective optimization model suitable for integration into a port DT
- From a digital twin development perspective, this thesis outlines:
  - The characteristics and requirements of ports
  - The need for interoperability

# Future work

- Provide further modeling components of a port digital twin
- Involve real operational data into our models
- Dive into the predictive maintenance aspect of port equipment



Many thanks for your attention!